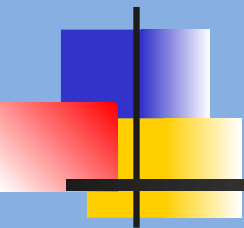


# Data Structures – Week #1



## Introduction



# Goals

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- We will learn methods of how to
  - (explicit goal) organize or **structure large amounts of data in the main memory (MM)** considering efficiency; i.e.,
    - *memory space* and
    - *execution time*
  - (implicit goal) gain additional experience on
    - what data structures to use for solving what kind of problems
    - programming



# Goals continued...1

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- **Explicit Goal**

- We look for answers to the following question:

“*How do we store data in MM* such that

1. *execution time* grows as *slow* as possible with the growing size of input data, and
2. data uses up *minimum memory space*?”

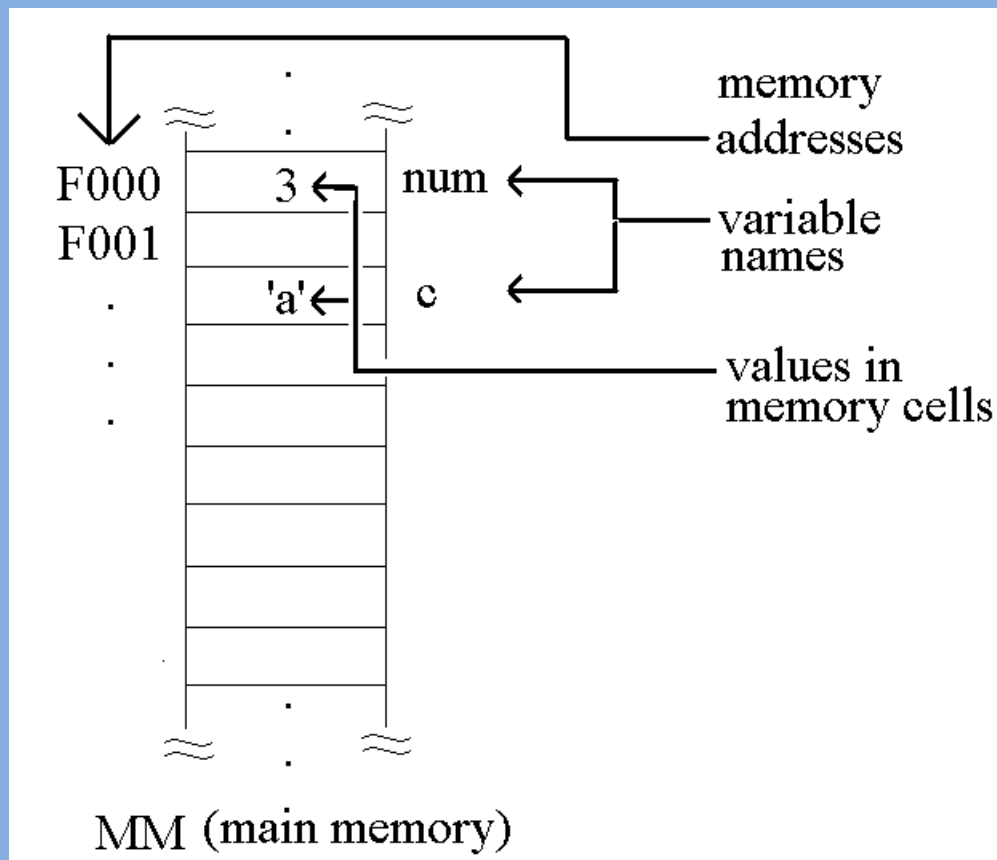


# Goals continued...2

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- As a tool to calculate the execution time of algorithms, we will learn the basic principles of **algorithm analysis**.
- To efficiently structure data in MM, we will thoroughly discuss the
  - *static*, (arrays)
  - *dynamic* (structures using pointers)ways of *memory allocations*, two fundamental implementation tools for data structures.

# Representation of Main Memory



# Examples for efficient vs. inefficient data structures



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- 8-Queen problem
  - 1D array vs. 2D array representation results in saving memory space
  - Search for proper spot (square) using horse moves save time over square-by-square search
- Fibonacci series: A lookup table avoids redundant recursive calls and saves time

# Examples for efficient vs. inefficient data structures

8-Queen problem (4-queen and 5-queen versions)

	X		
			X
X			
		X	



		X	
X			
			X
	X		

X				
		X		
				X
	X			
			X	



	X			
				X
		X		
X				
			X	

# Examples for efficient vs. inefficient data structures

## 8-Queen problem (4-q and 5-q versions)

	x		
			x
x			
		x	



```
int a[4][4];
```

```
....
```

```
a[0][1]=1;
```

```
a[1][3]=1;
```

```
a[2][0]=1;
```

```
a[3][2]=1;
```

inefficient:  
more memory  
space (16 bytes  
for 4-q version)  
required

x				
		x		
				x
	x			
			x	



```
int a[5];
```

```
....
```

```
a[0]=0;
```

```
a[1]=2;
```

```
a[2]=4;
```

```
a[3]=1;
```

```
a[4]=3;
```

efficient:  
less memory  
space (5 bytes  
for 5-q version)  
required





# Math Review

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## ■ Exponents

$$x^a x^b = x^{a+b}; \quad \frac{x^a}{x^b} = x^{a-b}; \quad (x^a)^b = x^{ab};$$

## ■ Logarithms

$$y = x^a \Leftrightarrow \log_x y = a, \quad y > 0; \quad \log_x y = \frac{\log_z y}{\log_z x}, \quad z > 0;$$

$$\log xy = \log x + \log y; \quad \log \frac{1}{x} = -\log x; \quad \log x^a = a \log x$$



# Math Review

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- Arithmetic Series: Series where the variable of summation is the base.

$$\sum_{i=1}^{k+1} i = \frac{k(k+1)}{2} + k + 1 = \frac{(k+1)(k+2)}{2};$$
$$\frac{k(k+1)}{2} + \frac{2(k+1)}{2} = \frac{(k+1)(k+2)}{2}$$



# Math Review

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- Geometric Series: Series at which the variable of summation is the exponent.

$$\sum_{i=0}^n a^i = \frac{1-a^{n+1}}{1-a}, \quad 0 < a < 1; \quad \sum_{i=0}^n a^i = \frac{a^{n+1}-1}{a-1}, \quad a \in \mathbb{N}^+ - \{1\};$$

$$\lim_{n \rightarrow \infty} \sum_{i=0}^n a^i = \frac{1}{1-a}, \quad 0 < a < 1;$$

$$s = \lim_{n \rightarrow \infty} \sum_{i=0}^n a^i = 1 + a + a^2 + a^3 + a^4 + \dots = \frac{1}{1-a};$$

$$as = \lim_{n \rightarrow \infty} a \sum_{i=0}^n a^i = a + a^2 + a^3 + a^4 + \dots = \frac{a}{1-a};$$

$$\Rightarrow s - as = s(1-a) = 1$$

# Math Review

- Geometric Series...cont'd
- An example to using above formulas to calculate another geometric series

$$s = \sum_{i=1}^{\infty} \frac{i}{2^i};$$

$$s = \frac{1}{2} + \frac{2}{2^2} + \frac{3}{2^3} + \cdots + \frac{i}{2^i} + \cdots$$

$$2s = 1 + \frac{2}{2} + \frac{3}{2^2} + \frac{4}{2^3} + \cdots + \frac{i}{2^{i-1}} + \cdots$$

$$s = 2s - s = 1 + \frac{1}{2} + \frac{1}{2^2} + \frac{1}{2^3} + \cdots + \frac{1}{2^i} + \cdots$$

$$s = \sum_{i=0}^{\infty} \frac{1}{2^i} = 2;$$

# Math Review

## ■ Proofs

### ■ Proof by Induction

#### ■ Steps

1. Prove the base case ( $k=1$ )
2. Assume hypothesis holds for  $k=n$
3. Prove hypothesis for  $k=n+1$

### ■ Proof by counterexample

- Prove the hypothesis wrong by an example

### ■ Proof by contradiction ( $A \Rightarrow B \Leftrightarrow \sim B \Rightarrow \sim A$ )

- Assume hypothesis is wrong,
- Try to prove this
- See the contradictory result

# Math Review

## ■ Proof examples (Proofs... cont'd)

### ■ Proof by Induction

#### ■ Hypothesis

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}$$

#### ■ Steps

1. Prove true for  $n=1$ :
2. Assume true for  $n=k$ :
3. Prove true for  $n=k+1$ :

$$\sum_{i=1}^1 i = 1$$

$$\sum_{i=1}^k i = \frac{k(k+1)}{2}$$

$$\sum_{i=1}^{k+1} i = \frac{k(k+1)}{2} + k + 1 = \frac{(k+1)(k+2)}{2};$$

$$\frac{k(k+1)}{2} + \frac{2(k+1)}{2} = \frac{(k+1)(k+2)}{2}$$



# Arrays

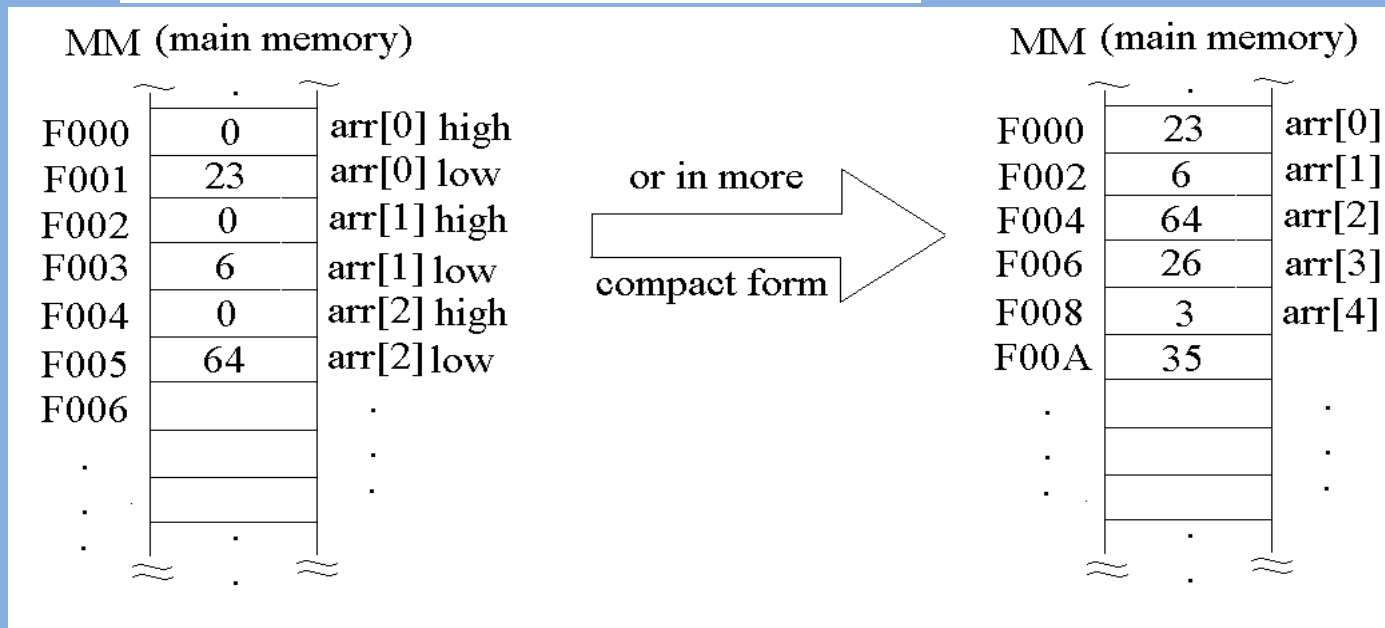
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- Static data structures that
  - represent **contiguous** memory locations holding **data of same type**
  - provide *direct access* to data they hold
  - have a *constant size* determined up front (at the beginning of) the run time

# Arrays... cont'd

- An **integer array example in C**
- `int arr[12]; //12 integers`

Index	→	0	1	2	3	4	5	6	7	8	9	10	11	
Value		23	6	64	26	3	35	8	56	39	48	41	12	arr







# Multidimensional Arrays

---

- To represent data with multiple dimensions, multidimensional array may be employed.
- Multidimensional arrays are structures specified with
  - the data value, and
  - as many indices as the dimensions of array
- Example:
  - `int arr2D[r][c];`



# Multidimensional Arrays

$$\begin{bmatrix} m[0][0] & m[0][1] & m[0][2] & \cdots & m[0][c-1] \\ m[1][0] & m[1][1] & m[1][2] & \cdots & m[1][c-1] \\ m[2][0] & m[2][1] & m[2][2] & \cdots & m[2][c-1] \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ m[r-1][0] & m[r-1][1] & m[r-1][2] & \cdots & m[r-1][c-1] \end{bmatrix}$$

- **$m$** : a two dimensional (2D) array with  $r$  rows and  $c$  columns
- **Row-major** representation: 2D array is implemented **row-by-row**.
- **Column-major** representation: 2D array is implemented **column-first**.
- In **row-major** rep.,  $m[i][j]$  is the entry of the above matrix  $m$  at  $i+1^{\text{th}}$  row and  $j+1^{\text{th}}$  column. “ $i$ ” and “ $j$ ” are row and column indices, respectively.
- How many elements?  $n = r * c$  elements

# Row-major Implementation

- Question: How can we store the matrix in a 1D array in a row-major fashion or how can we map the 2D array  $m$  to a 1D array  $a$ ?

$l$  elements

$a$	...	$m[0][0]$	...	$m[0][c-1]$	...	$m[r-1][0]$	...	$m[r-1][c-1]$	...
-----	-----	-----------	-----	-------------	-----	-------------	-----	---------------	-----

*index:*  $k \rightarrow$      $k=l$                        $k=l+c-1$                        $k=l+(r-1)c+0$      $k=l+(r-1)c+c-1$

In general,  $m[i][j]$  is placed at  $a[k]$  where  $k=l+ic+j$ .



# Implementation Details of Arrays

---

1. *Array names are pointers* that point to the first byte of the first element of the array.
  - a) `double vect[row_limit];` // vect is a pointer!!!
2. *Arrays* may be efficiently *passed to functions* using their *name* and their *size* where
  - a) the name specifies the beginning address of the array
  - b) the size states the bounds of the index values.
3. Arrays can only be copied element by element.



# Implementation Details... cont'd

---

```
#define maxrow ...;
#define maxcol ...;
...
int main()
{
    int minirow;
    double min;
    double probability_matrix[maxrow][maxcol];
    ... ; //probability matrix initialized!!!
    min=minrow(probability_matrix,maxrow,maxcol,&minirow);
    ...
    return 0;
}
```



# Implementation Details... cont'd

---

```
double minrow(double darr[][maxcol], int xpos, int ypos, int *ind)
{ // finds minimum of sum of rows of the matrix and returns the sum
  // and the row index with minimum sum.
  double mn;
  ...
  mn=<a large number>;
  for (i=0; i<=xpos; i++) {
    sum=0;
    for (j=0; j<=ypos; j++)
      sum+=darr[i][j];
    if (mn > sum) { mn=sum; *ind=i; } // call by reference!!!
  }
  return mn;
}
```



# Records (Structures)

---

- As opposed to **arrays** in which we keep **data of the same type**, we keep related data of various types in a **record**.
- **Records** are used to encapsulate (keep together) related data.
- **Records** are composite, and hence, **user-defined data types**.
- In **C**, records are formed using the reserved word “**struct**.”



# Struct

---

- We declare as an example a student record called “stdType”.
- We declare first the data types required for individual fields of the record `stdType`, and then the record `stdType` itself.





# Struct... Example

---

```
enum genderType = {female, male}; // enumerated type declared...
typedef enum genderType genderType; // name of enumerated type shortened...
struct instrType {
    ...                               //left for you as exercise!!!
}
```

```
typedef struct instrType instrType;
struct classType { // fields (attributes in OOP) of a course declared...
    char classCode[8];
    char className[60];
    instrType instructor;
    struct classtype *clsPtr;
}
typedef struct classType classType; // name of structure shortened...
```



# Struct... Example continues

---

```
struct stdType {  
    char id[8];                //key  
    //personal info  
    char name[15];  
    char surname[25];  
    genderType gender;        //enumerated type  
    ...  
    //student info  
    classType current_classes[10]; //...or      class_type *cur_clsptr  
    classType classes_taken[50];  //...or class_type *taken_clsptr  
    float grade;  
    unsigned int credits_earned;  
    ...  
    //next record's first byte's address  
    struct stdType *sptr;        //address of next student record  
}
```



# Memory Issues

---

- Arrays can be used within records.
  - Ex: `classType current_classes[10];` // from previous slide
- Each element of an array can be a record.
  - `stdType students[1000];`
- Using an array of `classType` for keeping taken classes wastes memory space (Why?)
  - Any alternatives?
- How will we keep student records in MM?
  - In an array?
  - Advantages?
  - Disadvantages?



# Array Representation

## Advantages

1. Direct access (i.e., faster execution)

## Disadvantages

1. Not suitable for changing number of student records
  - The higher the extent of memory waste the smaller the number of student records required to store than that at the initial case.
  - The (constant) size of array requires extension which is impossible for static arrays in case the number exceeds the bounds of the array.

The other alternative is **pointers** that provide **dynamic memory allocation**

indices	0	1	2	...	...	n-3	n-2	n-1
students	std 1	std 2	std 3	...	...	std n-2	std n-1	std n

Array Representation

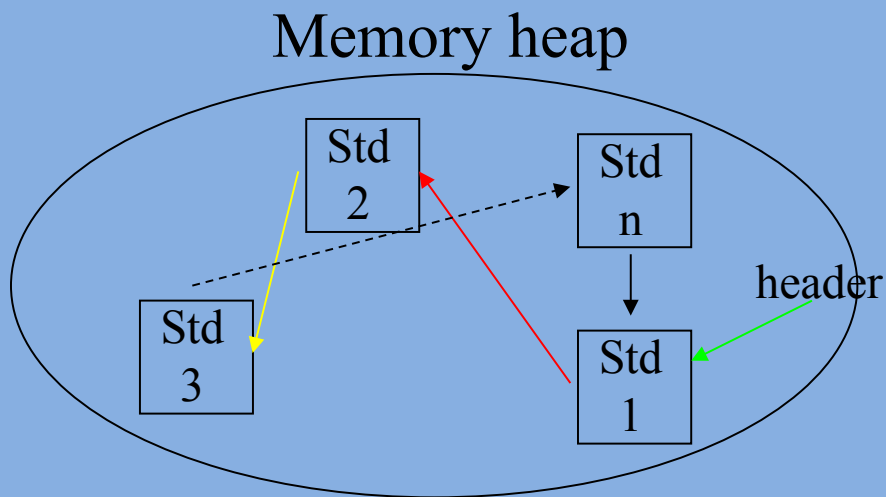
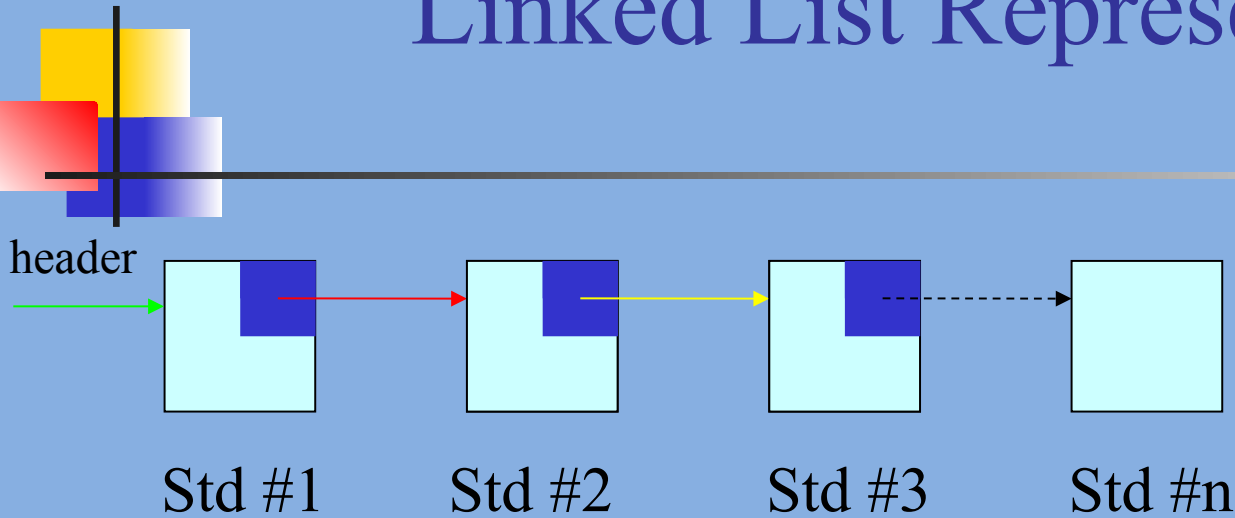


# Pointers

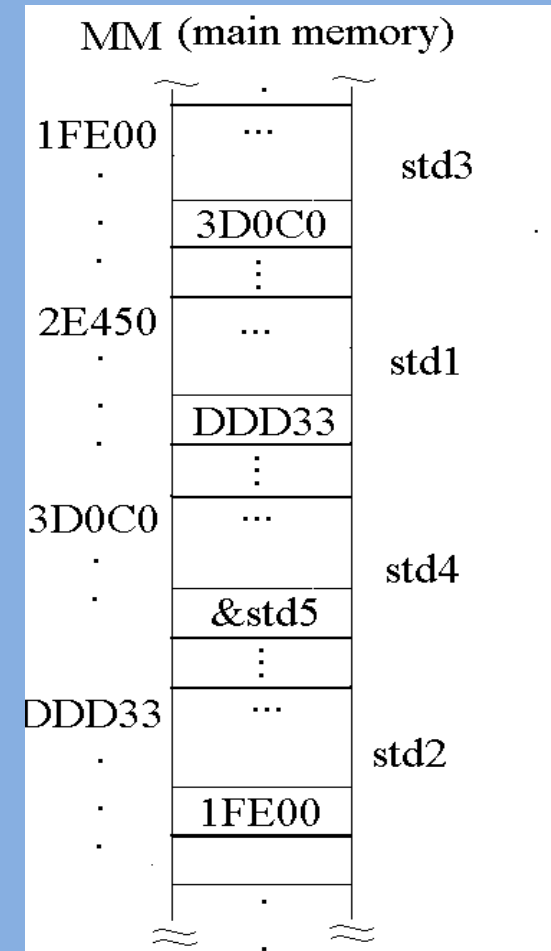
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- Pointers are variables that hold memory addresses.
- Declaration of a pointer is based on the type of data of which the pointer holds the memory address.
  - Ex: `stdtype *stdptr;`

# Linked List Representation

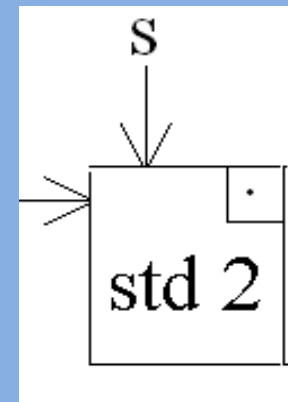
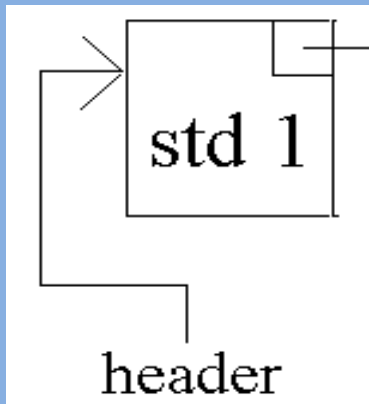


Value of header=**2E450**



# Dynamic Memory Allocation

```
header=(*stdtype) malloc(sizeof(stdtype));  
//Copy the info of first student to node pointed to by header  
s=(*stdtype) malloc(sizeof(stdtype));  
//Copy info of second student to node pointed to by header  
Header->sptr=s;  
...
```





# Arrays vs. Pointers

---

- Static data structures
- Represented by an index and associated value
- Consecutive memory cells
- Direct access (+)
- Constant size (-)
- Memory not released during runtime (-)
- Dynamic data structures
- Represented by a record of information and address of next node
- Randomly located in heap (cause for need to keep address of next node)
- Sequential access (-)
- Flexible size (+)
- Memory space allocatable and releasable during runtime (+)